

Mechanics of Earthquakes and Faulting

Lecture 13 , 16 Mar. 2021

www.geosc.psu.edu/Courses/Geosc508

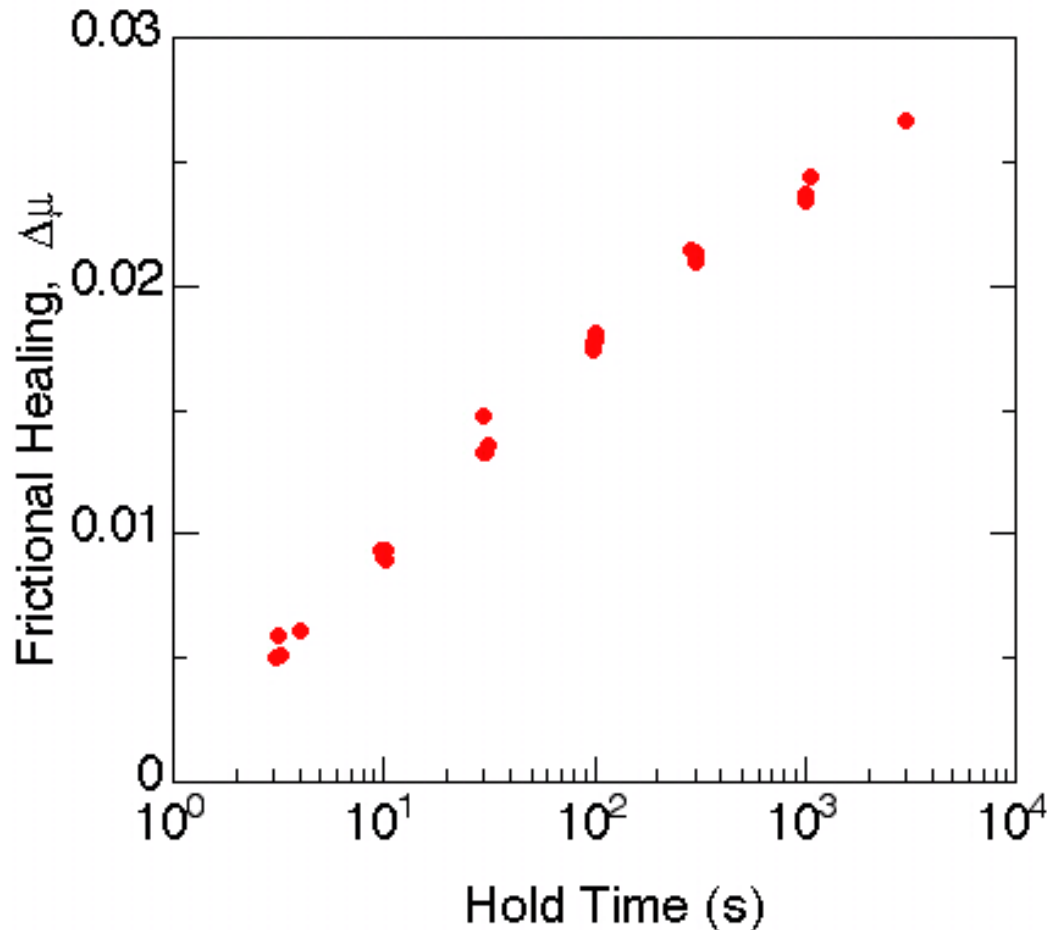
- Frictional healing. Aging and rate state friction. Application to tectonic faults and measurements of fault healing
- Normal stress oscillations and the critical vibration period for friction
- Healing: Affect of loading rate, shear stress, chemical environment, granular packing --Stressed vs. unstressed frictional aging
- Next time: role of healing for connecting friction to fracture mechanics
- Slow earthquakes and the opportunity to further investigate the application of rate state friction laws to instability.
- Recent lab work showing repetitive stick-slip instability for the complete spectrum of slip behaviors – A new opportunity to investigate the mechanics of slow slip
- Mechanisms: Why are they slow?
- Quasi-dynamic frictional instability (positive feedback, self-driven instability)

Rate (v) and State (θ) Friction Constitutive Laws

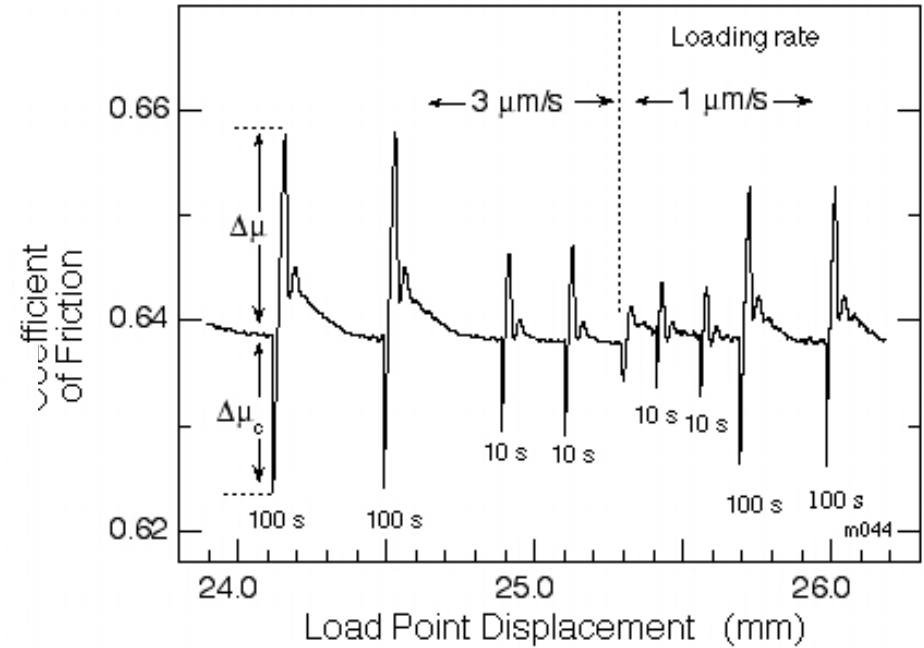
$$1) \quad \mu(\theta, V) = \mu_o + a \ln \left(\frac{V}{V_o} \right) + b \ln \left(\frac{V_o \theta}{D_c} \right)$$

$$2) \quad \frac{d\theta}{dt} = 1 - \frac{V\theta}{D_c}$$

$$3) \quad \frac{d\mu}{dt} = k(V_{lp} - V) \quad \text{Elastic Coupling}$$



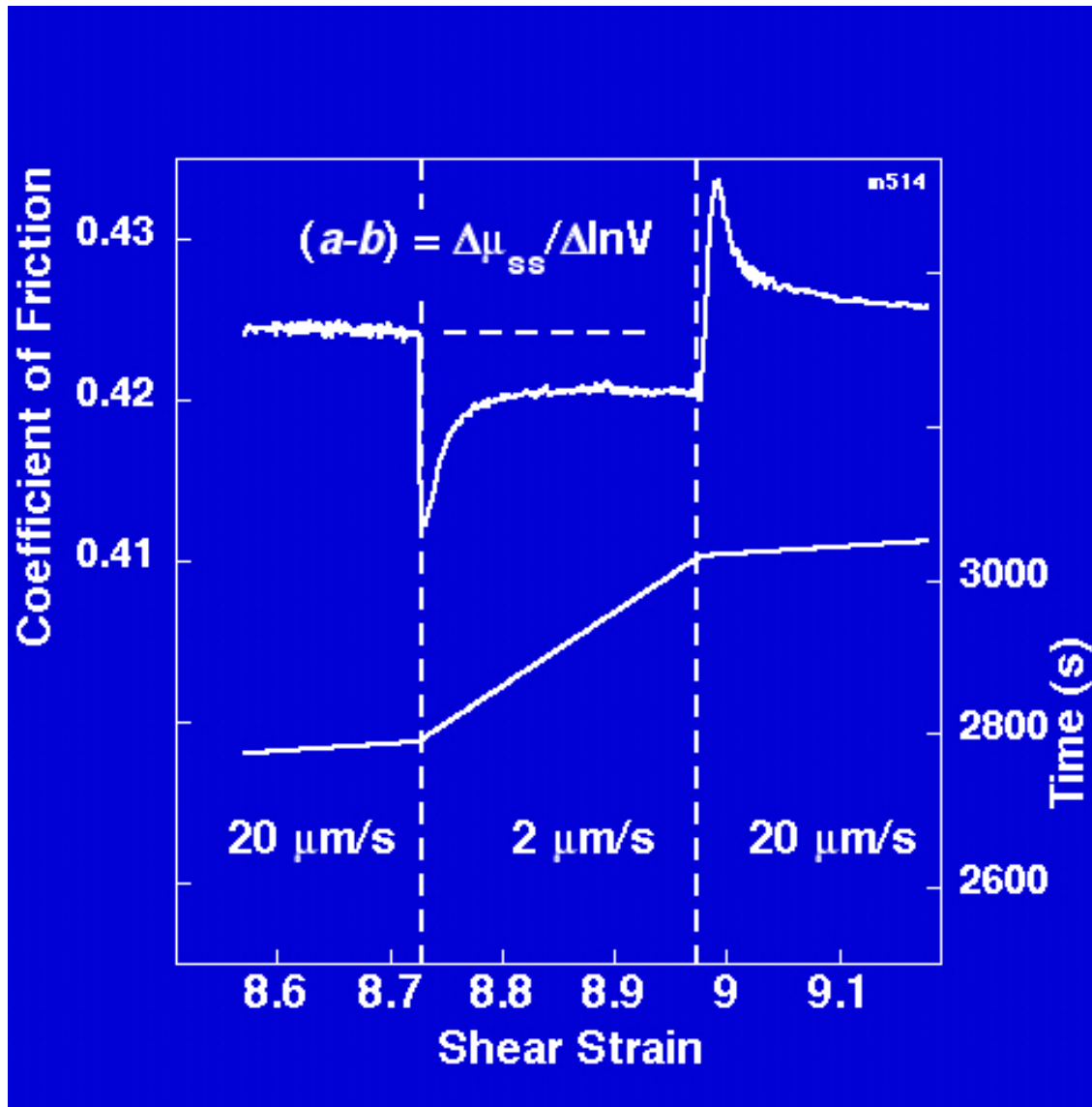
Modeling experimental data



$$\frac{d\mu}{dt} = k(V_{lp} - V)$$

Measuring the velocity dependence of friction

Frictional Instability
Requires $(a-b) < 0$



Constitutive Modelling

Rate and State Friction Law

Elastic Interaction, Testing Apparatus

$$\mu(\theta, v) = \mu_0 + a \ln\left(\frac{v}{v_0}\right) + b \ln\left(\frac{v_0 \theta}{D_c}\right)$$

$$\frac{d\theta}{dt} = 1 - \frac{v\theta}{D_c}$$

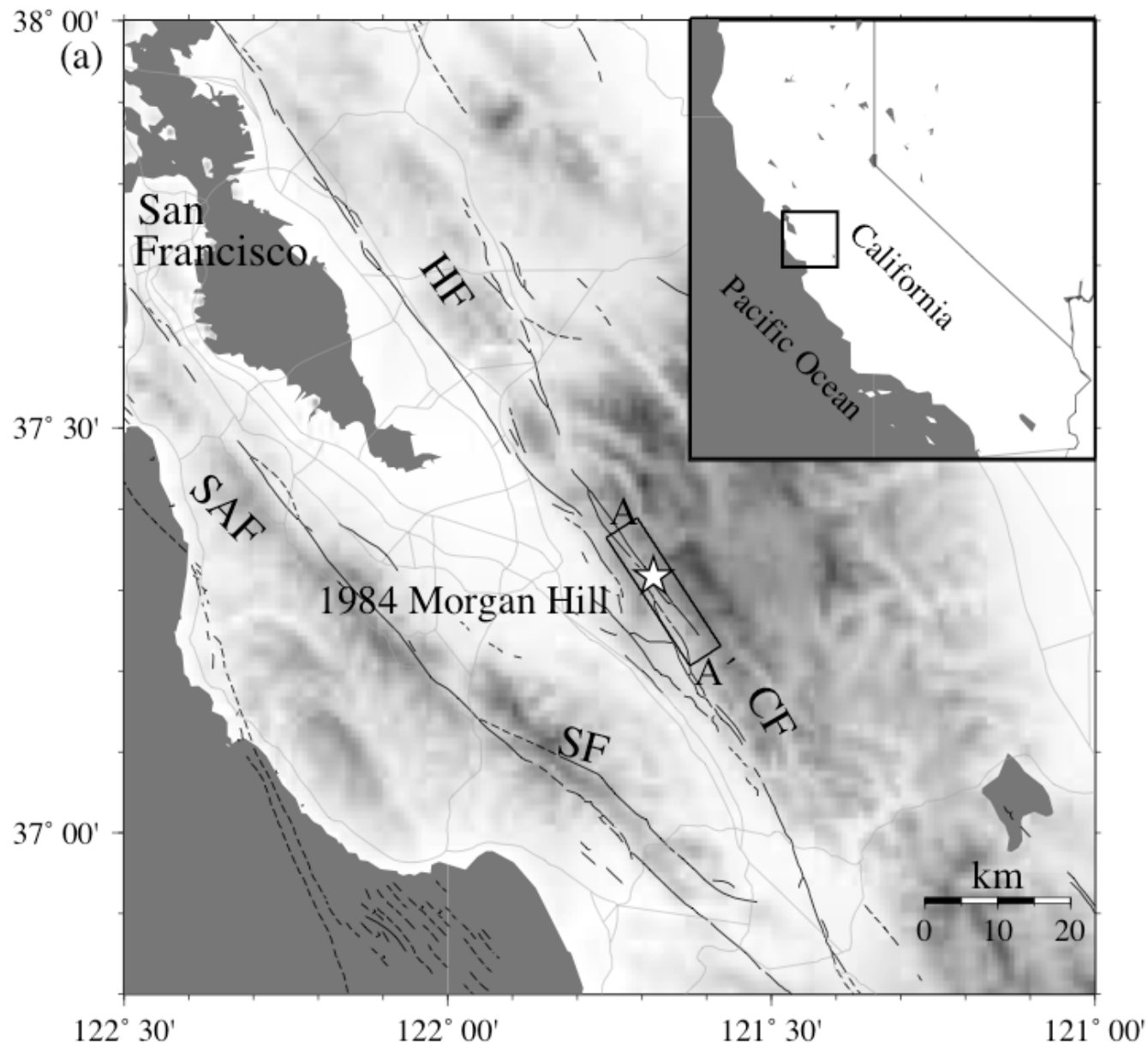
$$\theta_{ss} = \frac{D_c}{v}$$

$$\Delta\mu_{ss} = (a-b) \ln\left(\frac{v}{v_0}\right)$$

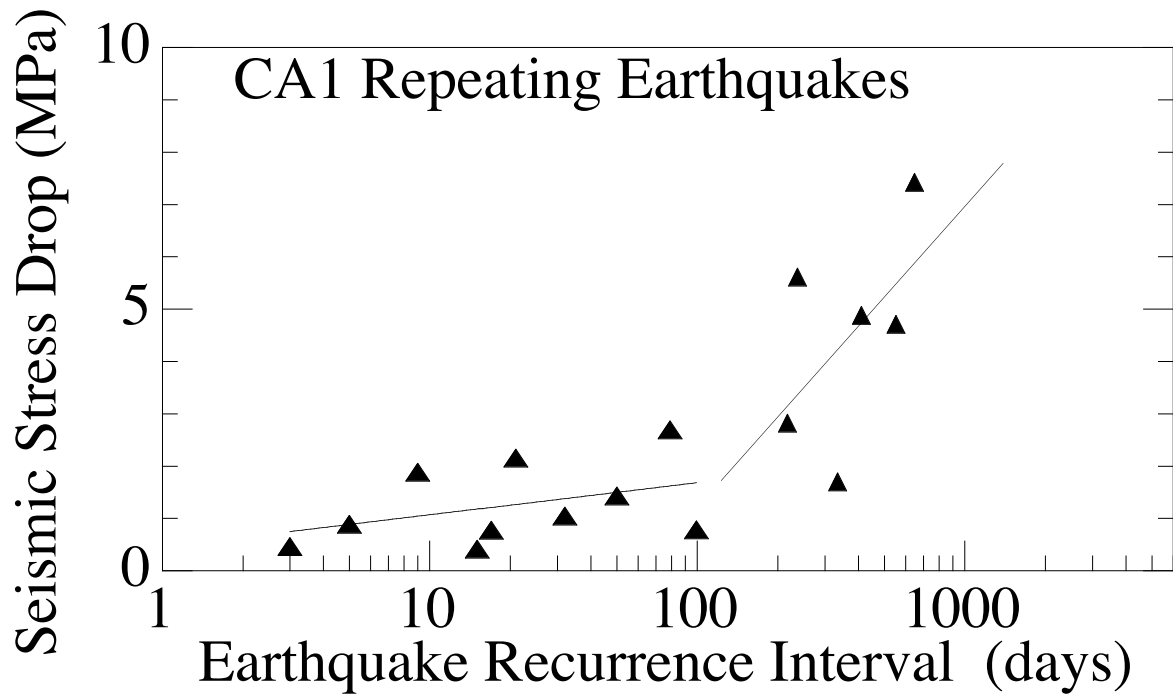
$$\frac{d\mu}{dt} = k' (v_{lp} - v)$$

Fault Healing and the Seismic Cycle: Repeating Earthquakes

How do faults regain strength between earthquakes?



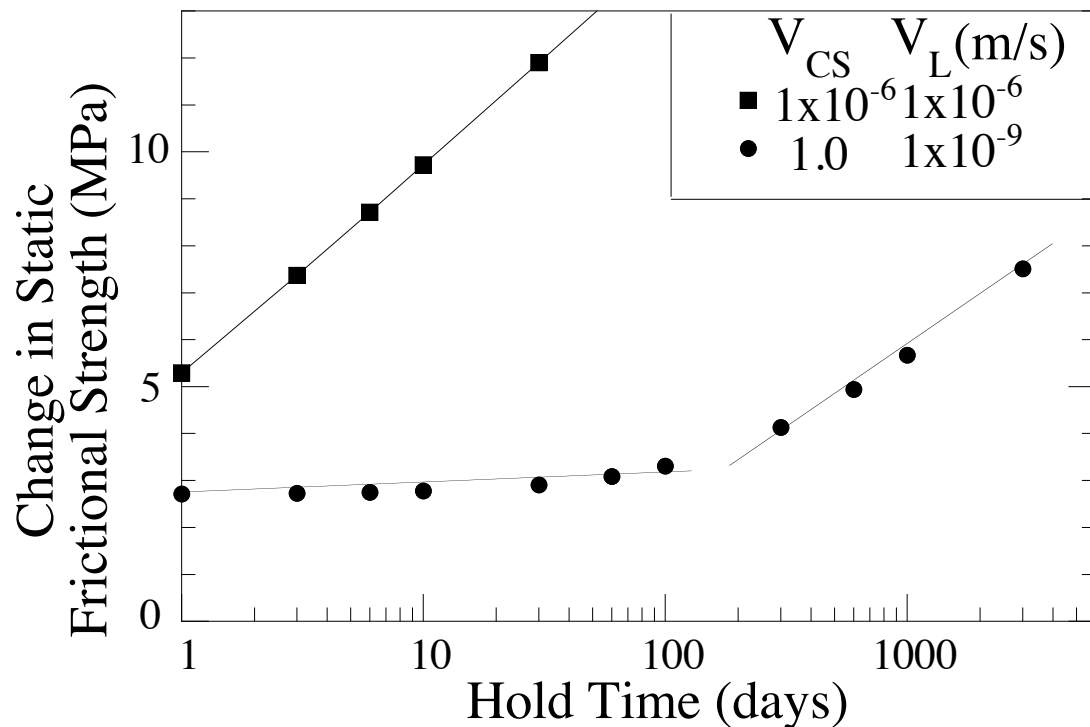
Vidale et al., 1994; Peng, Vidale, Marone & Rubin, GRL 2005



Assuming:

- Lab values for friction parameters a and b
- Lab & Field-based estimate of D_c
 - D_c proportional to shear zone width
- Stiffness $k \sim G/r$

Numerical Simulations



Healing rate of Calaveras repeaters agrees with room-T friction experiments, and shows predicted break in slope due to initial, rapid postseismic slip.

Earthquakes:

$\Delta\tau \sim 2$ MPa per decade in time

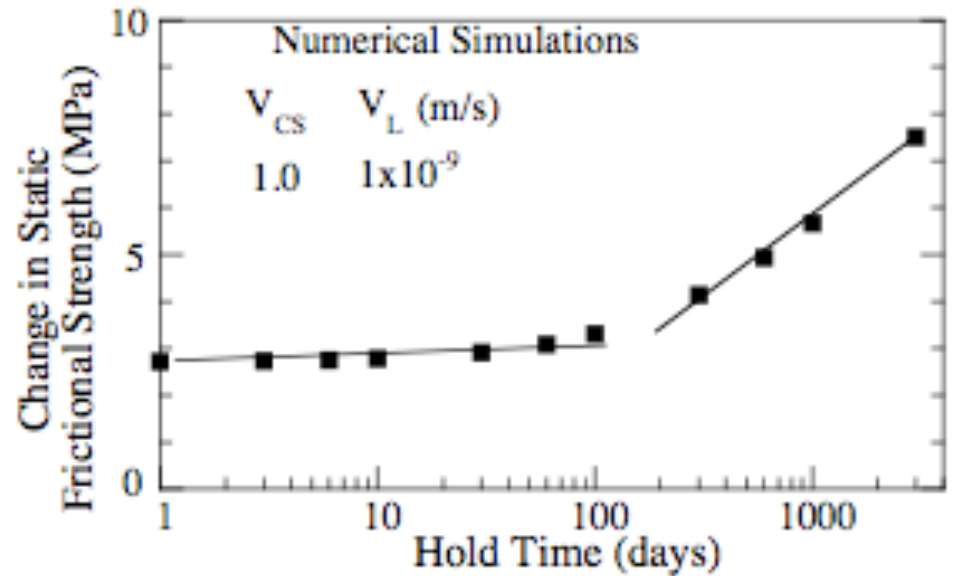
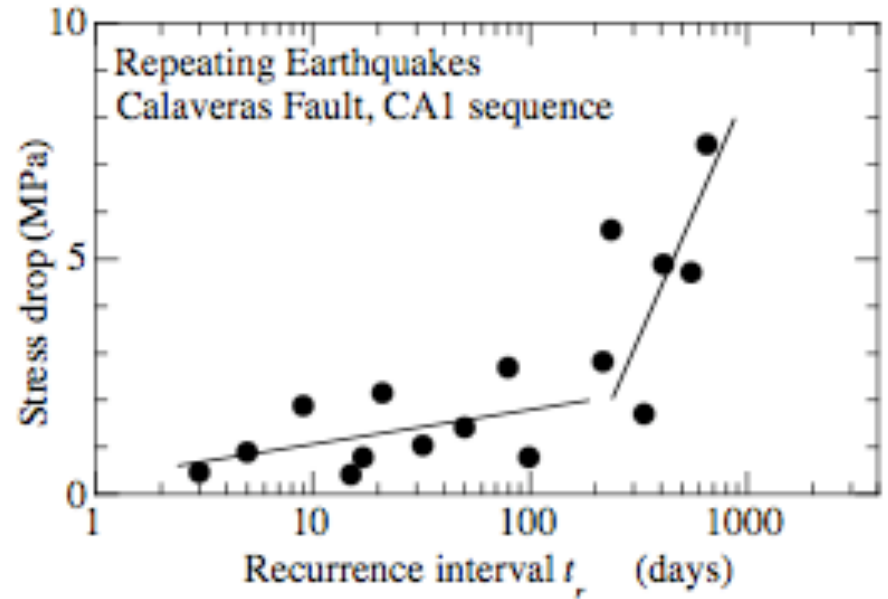
Lab Friction Experiment

$\Delta\mu \sim 0.01$ per decade in time

$\sigma \sim 100$ MPa

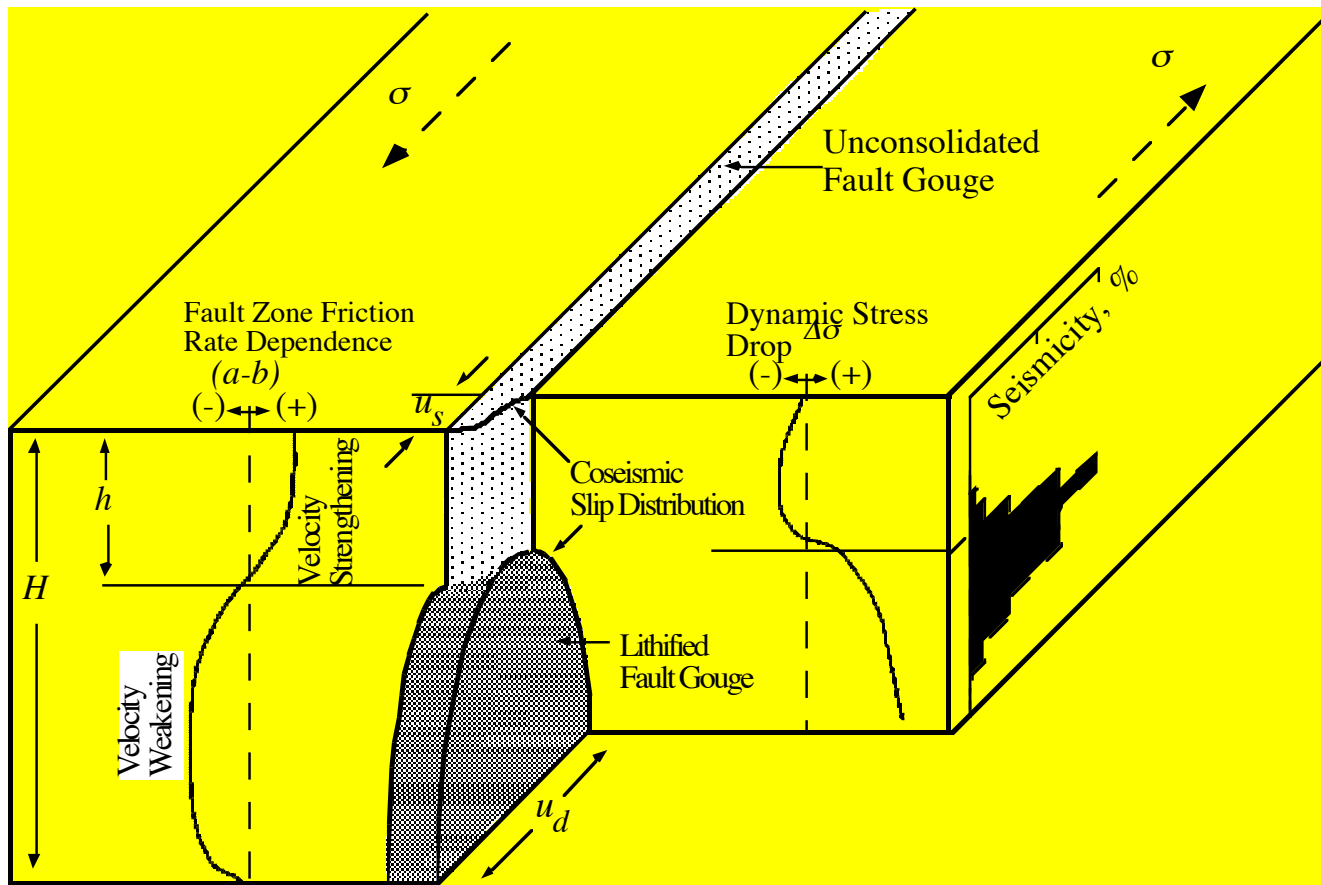
$\Delta\tau = \sigma \Delta\mu$

$\Delta\tau \sim 1$ MPa per decade in time



Marone, Nature, 1998

- Frictional healing: Time dependent, chemically-assisted mechanism, slip rate matters, shear stress level matters
- Fault healing: old faults are strong, earthquake stress drop increases with log recurrence time for major tectonic faults.
- Repeating earthquakes: small events, complex behavior



(a-b)

+	aseismic zone
-	Seismogenic zone
+	aseismic zone

Modeling the effect of normal force vibration 1.

Rate and State Friction Theory

$$\mu(\theta, v, \sigma) = \mu_0 + a \ln\left(\frac{v}{v_0}\right) + b \ln\left(\frac{v_0 \theta}{D_c}\right)$$

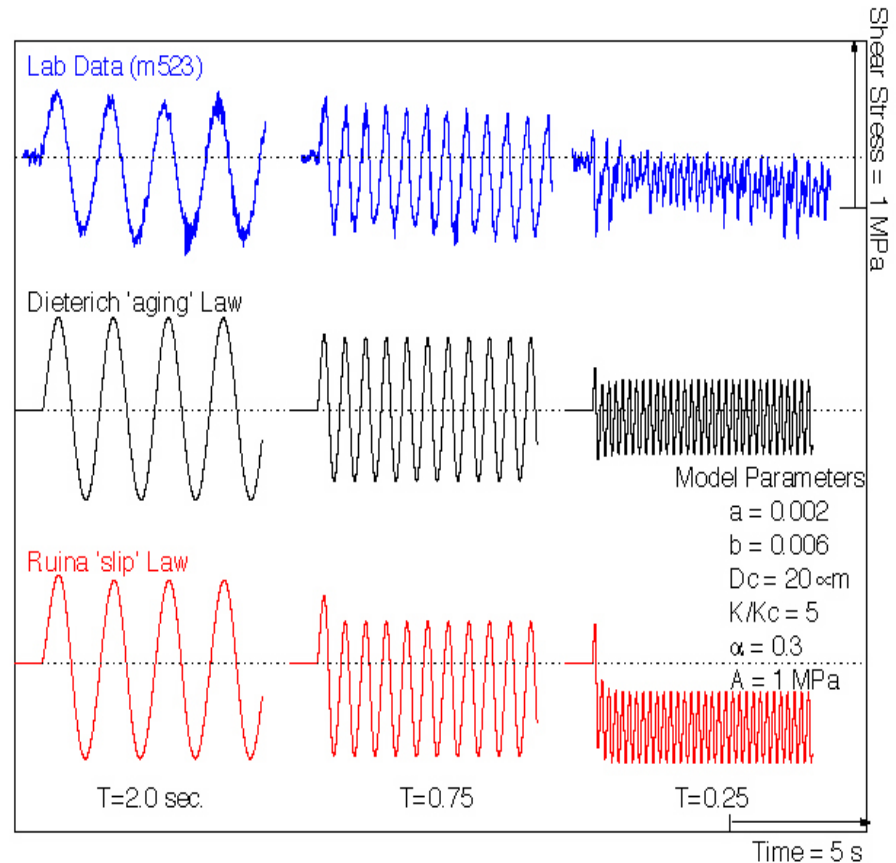
$$\frac{d\theta}{dt} = 1 - \frac{v\theta}{D_c} \quad \text{Dieterich Law}$$

$$\theta = \theta_0 \left(\frac{\sigma_{initial}}{\sigma_{final}}\right)^{\frac{\alpha}{b}} \quad \text{Normal Stress}$$

$$\frac{d\mu}{dt} = k' (v_{lp} - v) \quad \text{Elastic Coupling}$$

$$T_c = 2\pi \frac{D_c}{V} \sqrt{\frac{a}{b-a}} \quad \text{Critical Vibration Period}$$

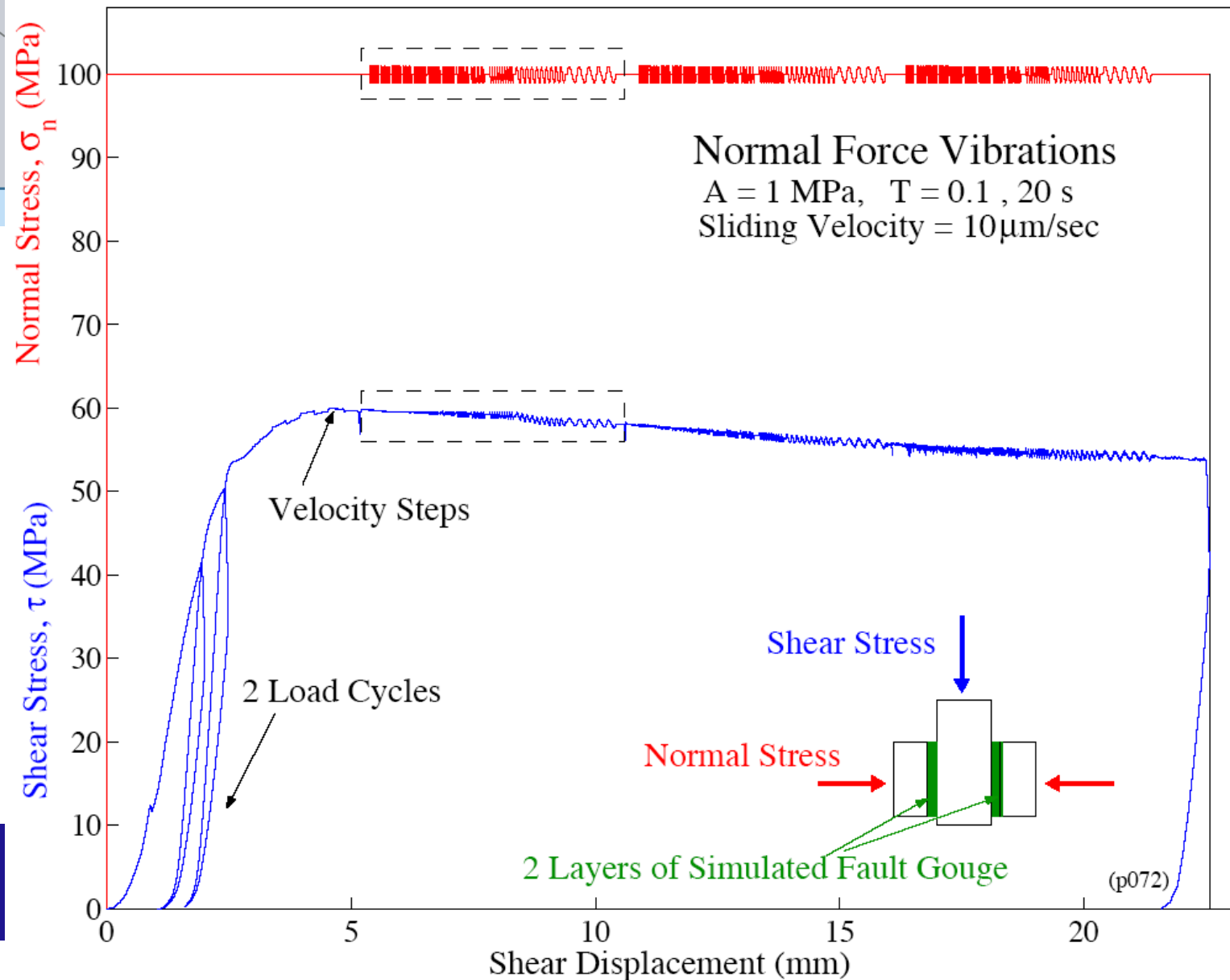
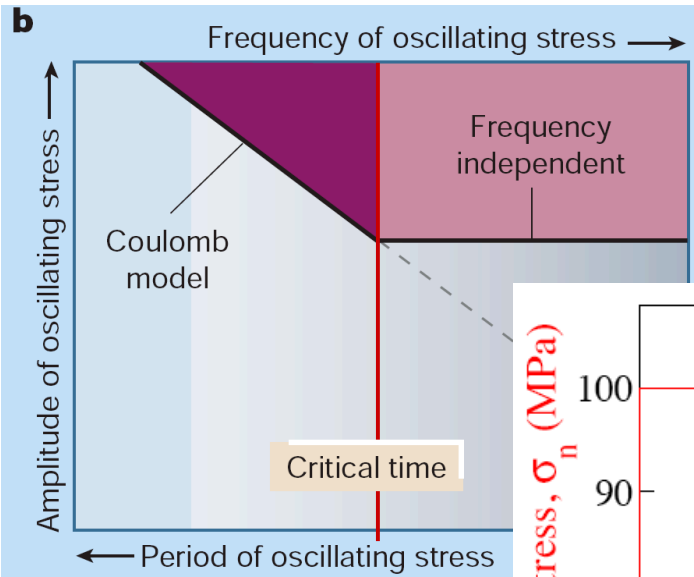
$$K_c = \sigma \frac{(b-a)}{D_c} + \frac{m v_0^2 (b-a)}{D_0^2} \quad \text{Critical Stiffness}$$



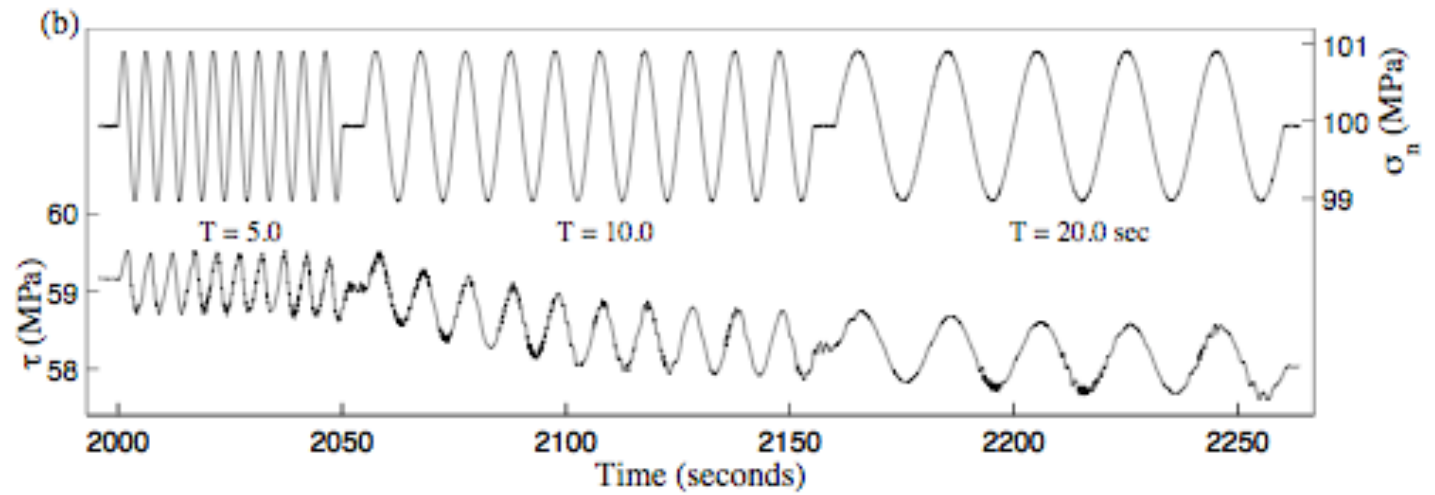
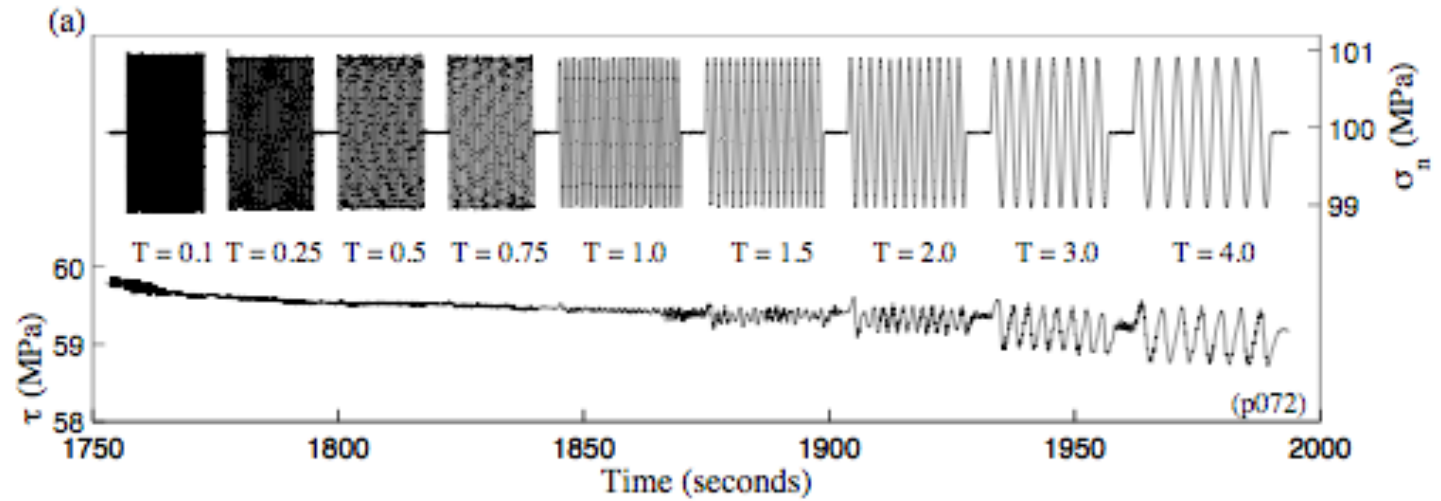
$T_c \sim$ time needed to slip a distance D_c

Lab: Normal Stress Vibrations

Critical period observed



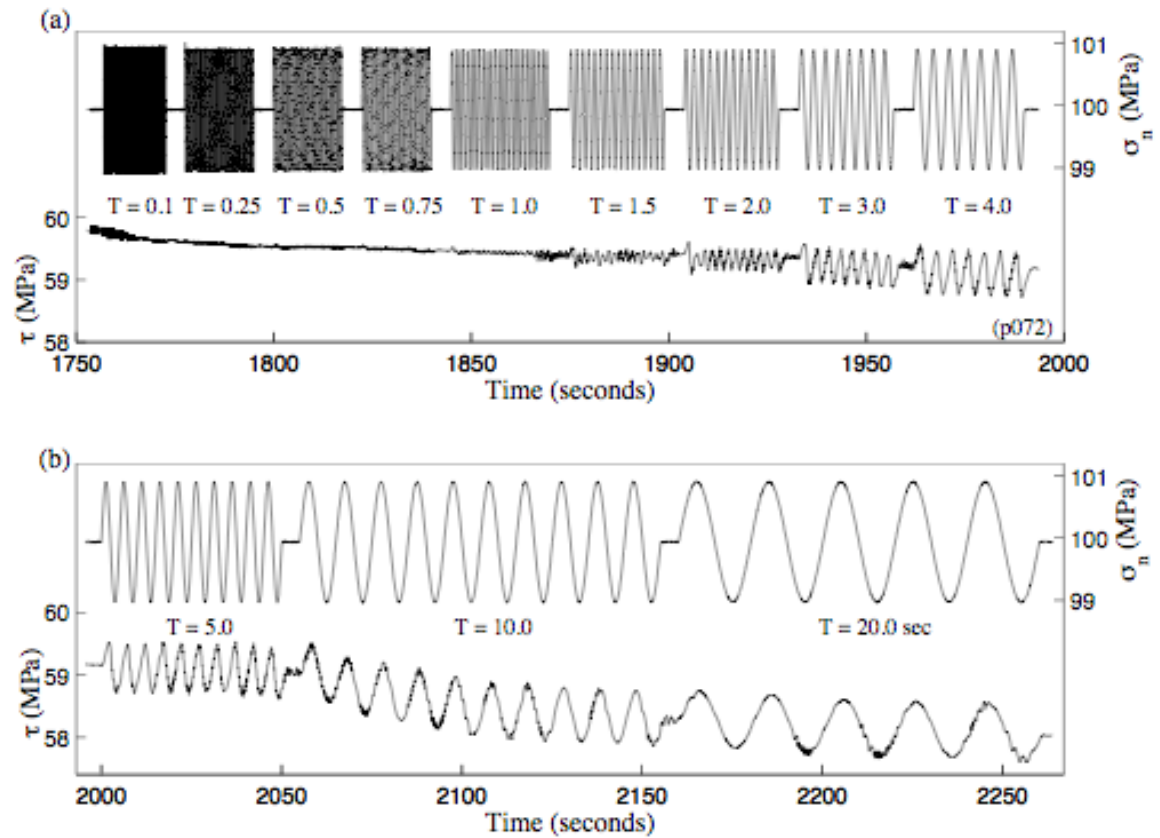
Boettcher &
Marone, JGR, 2004



Critical period is 1 to 2 sec.

*Critical Vibration
Period*

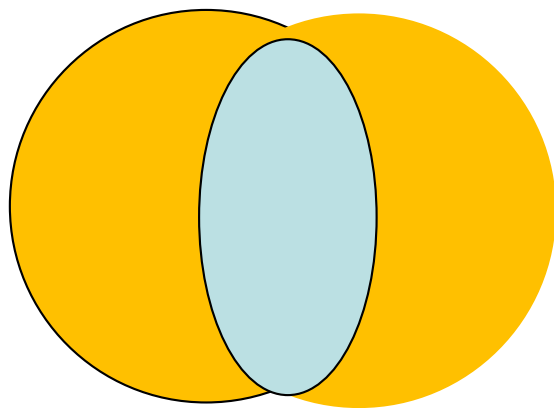
$$T_c = 2\pi \frac{D_c}{V} \sqrt{\frac{a}{b-a}}$$



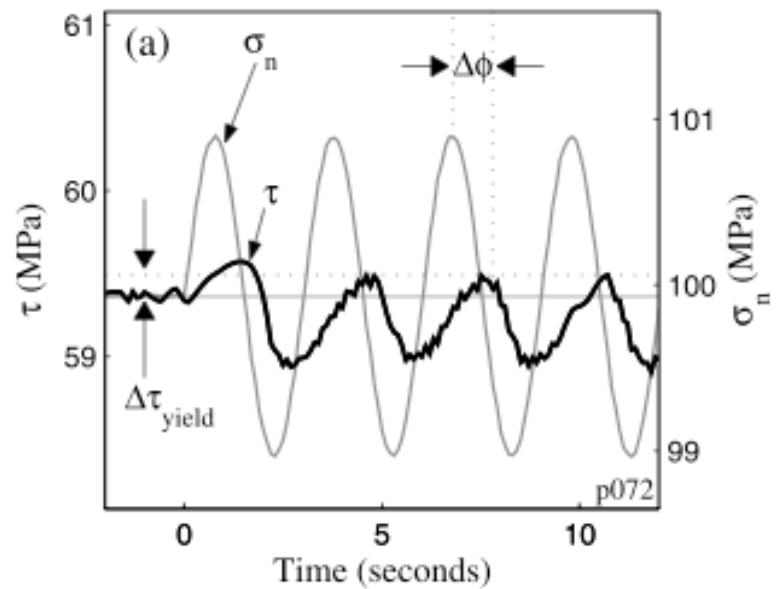
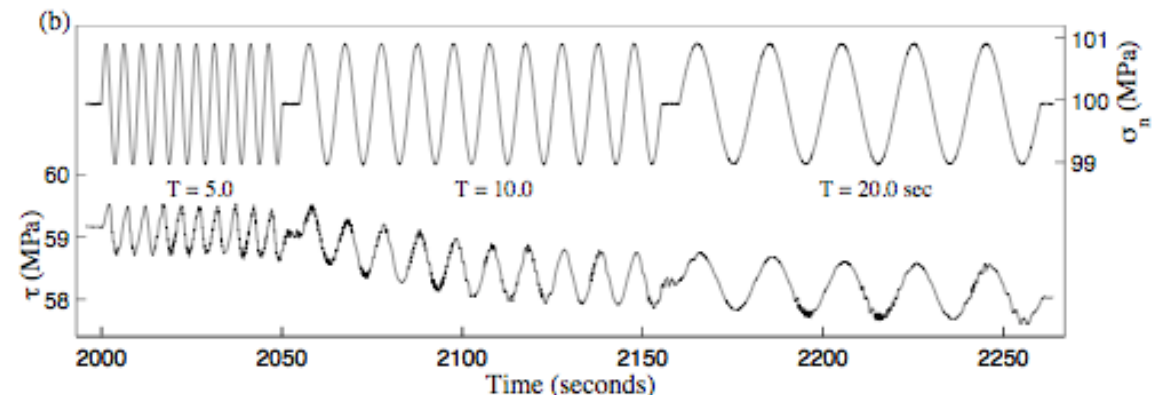
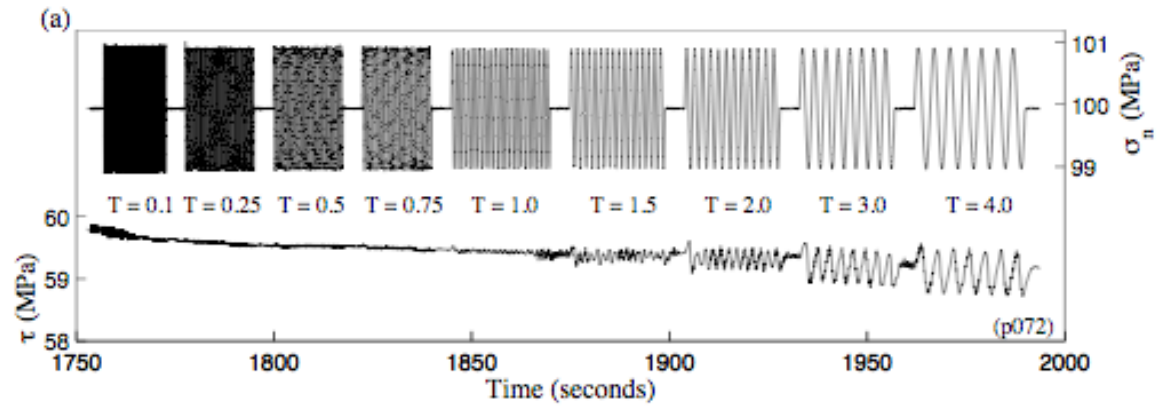
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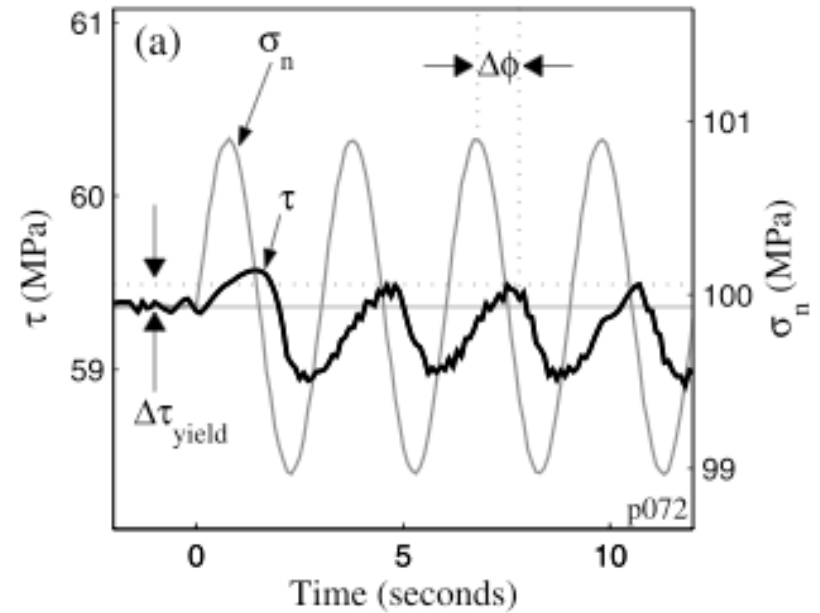
$$T_c = 2\pi \frac{D_c}{V} \sqrt{\frac{a}{b-a}}$$



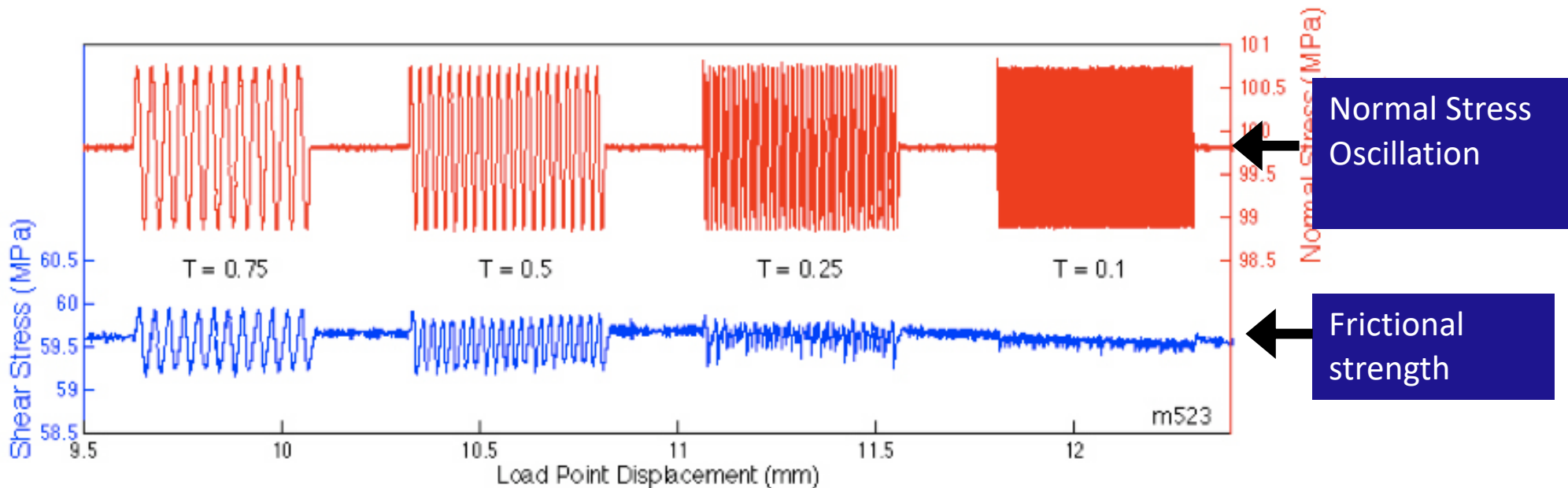
Time needed to slip a distance $D_c = D_c/V$



Also, Phase lag.
Friction response lags
stressing.
Could explain delayed
triggering

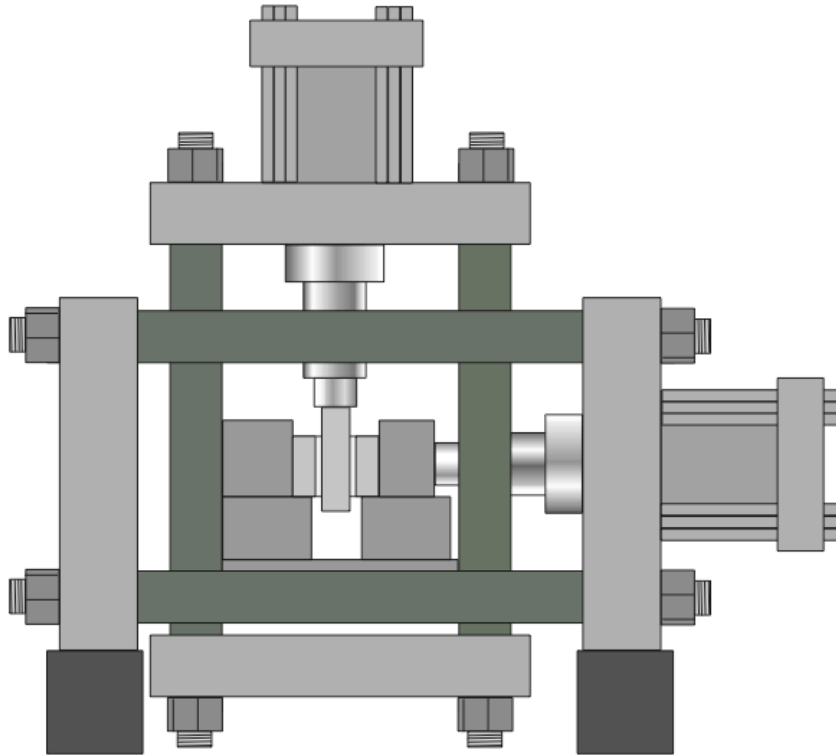


No frictional response to high frequency oscillations

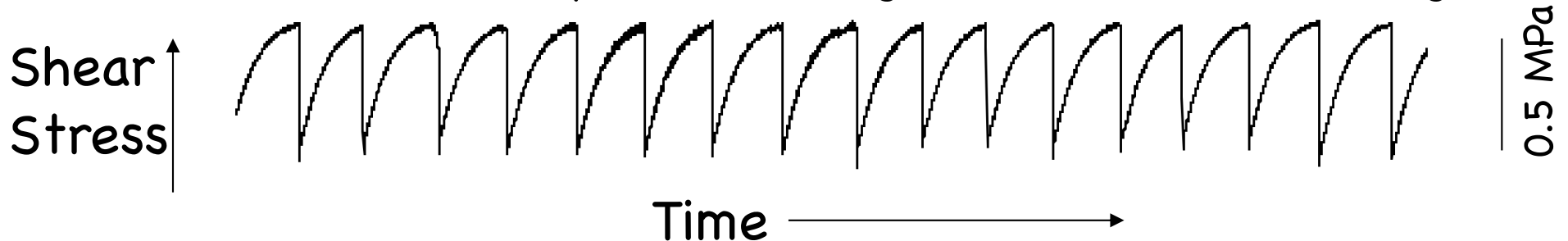


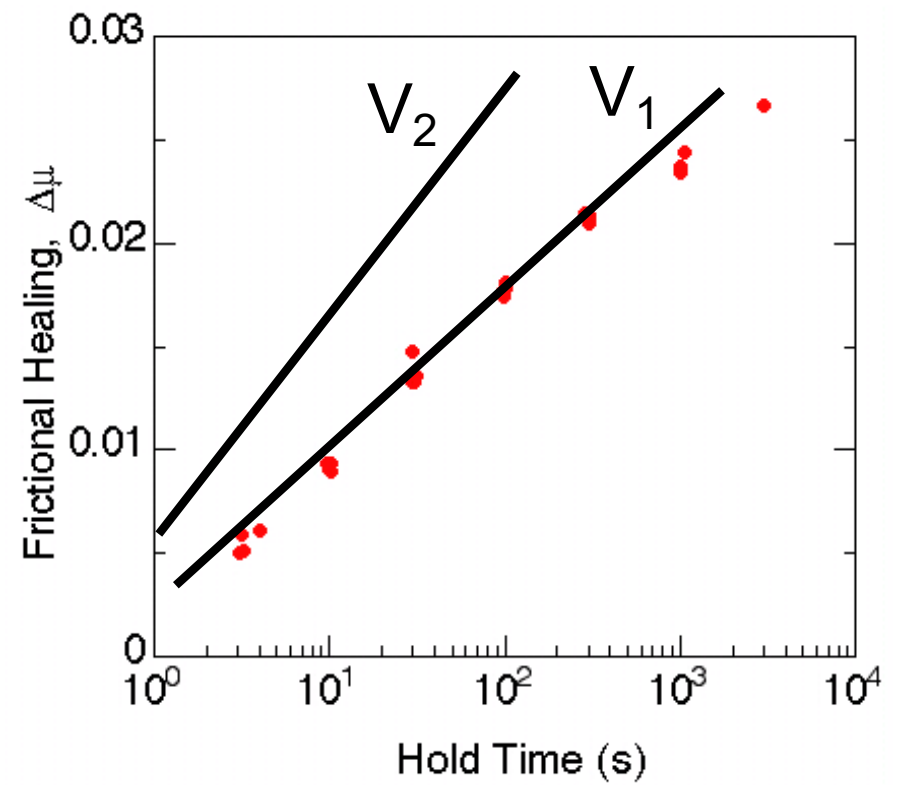
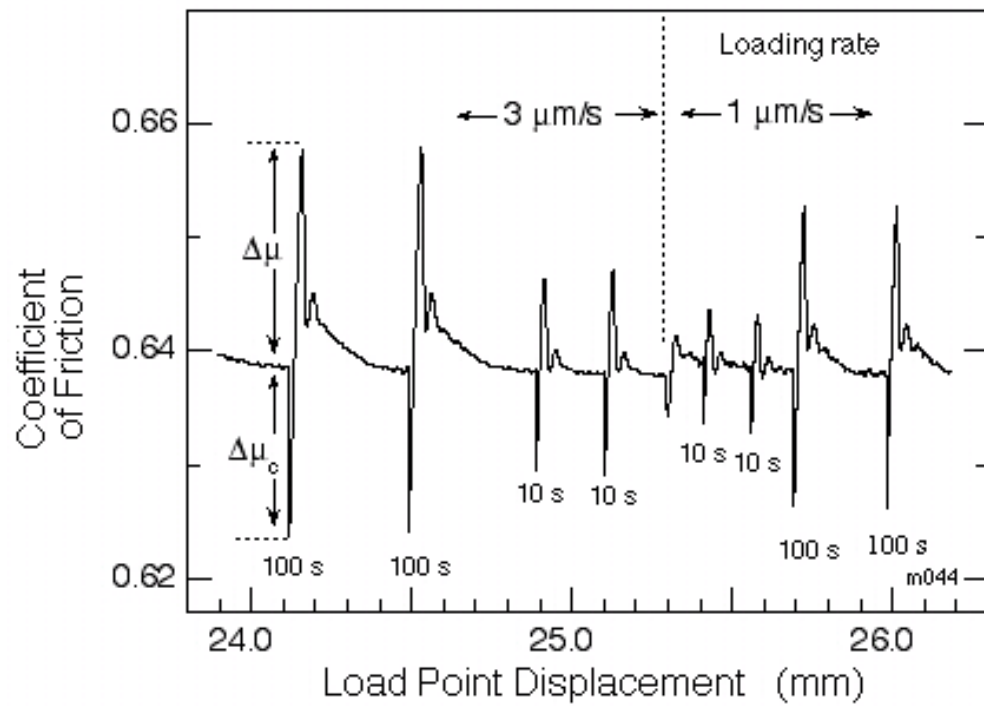
How do fault/frictional surfaces heal (regain strength) after failure?

Earthquakes & Fault Mechanics:
seismic cycle, fault reactivation.
*(friction and stick slip: doors,
windows, machines, ships in dry
dock, dancers...)*



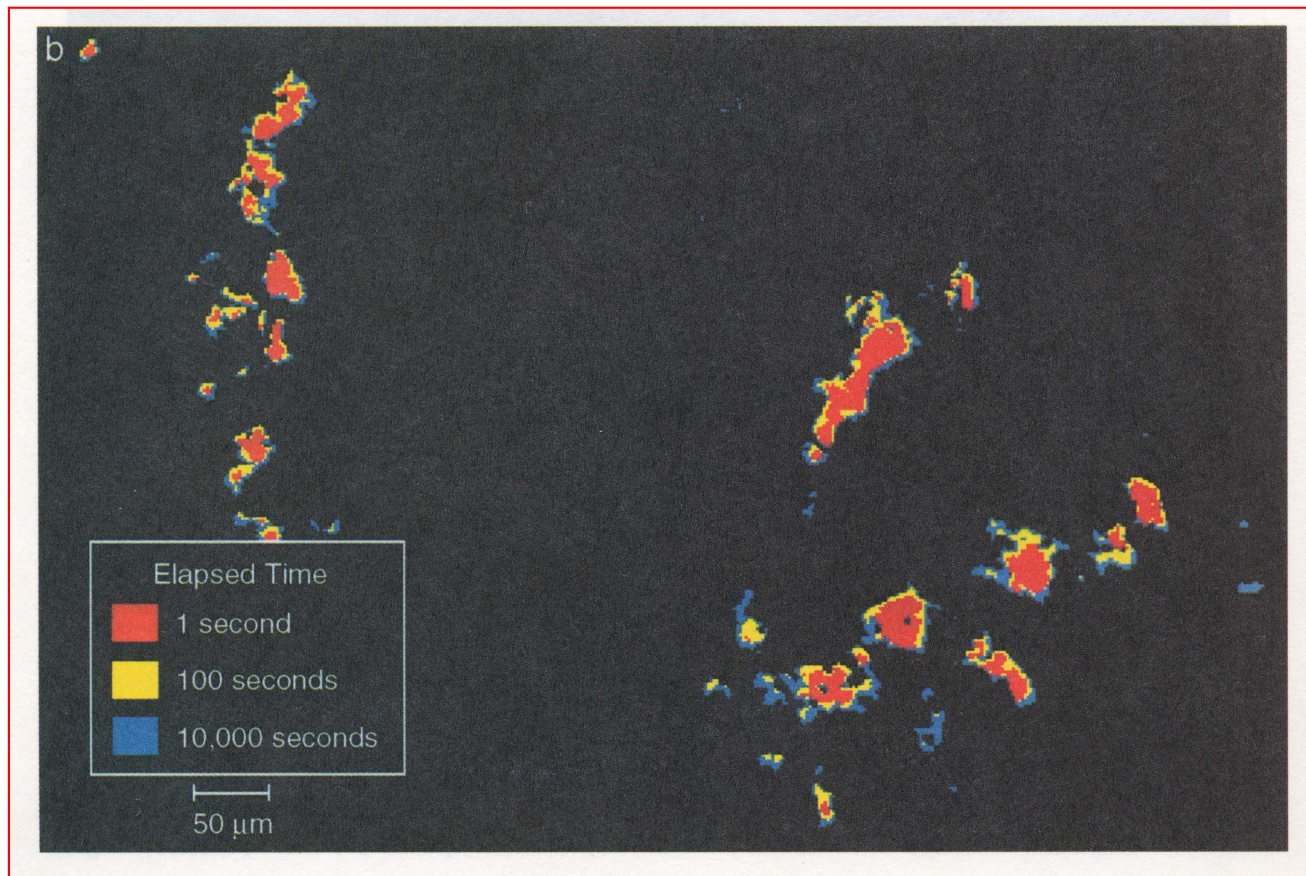
Stick-slip failure during shear at constant loading rate





Frictional aging.

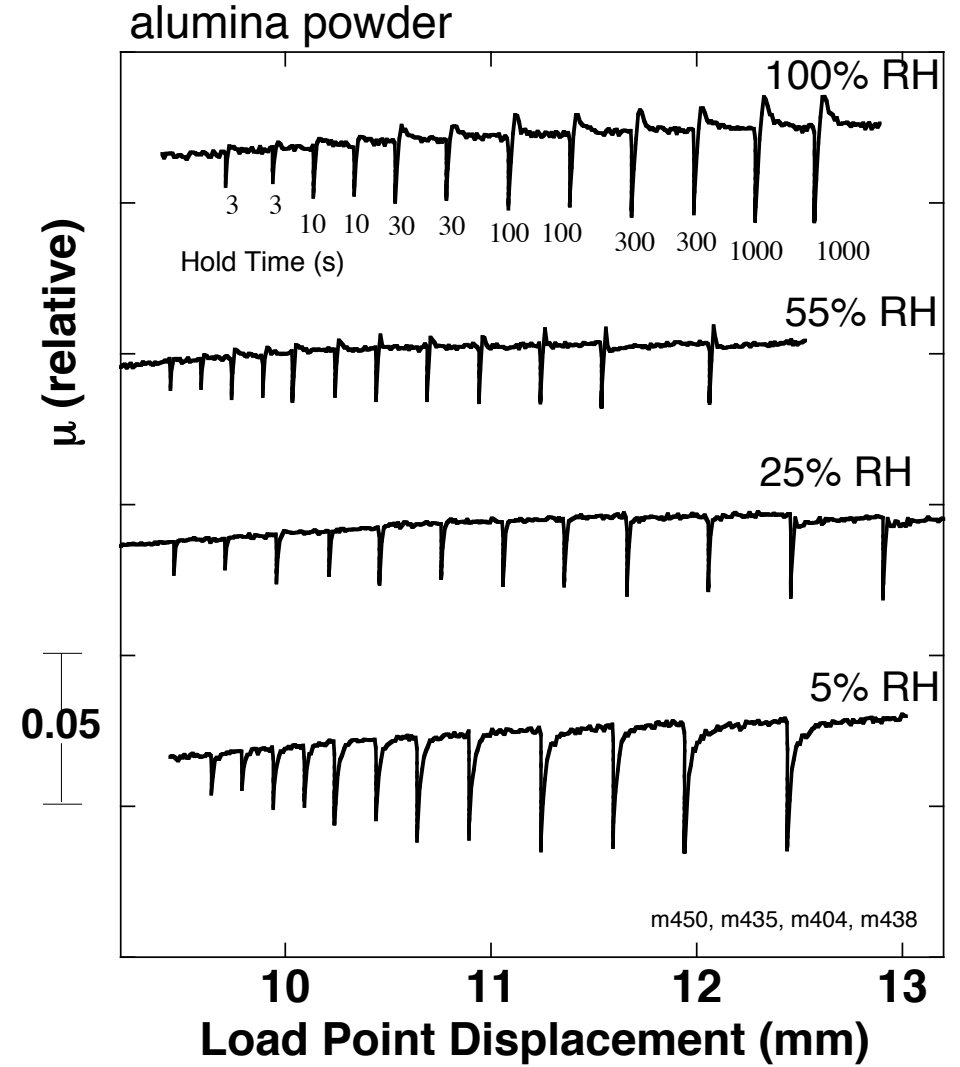
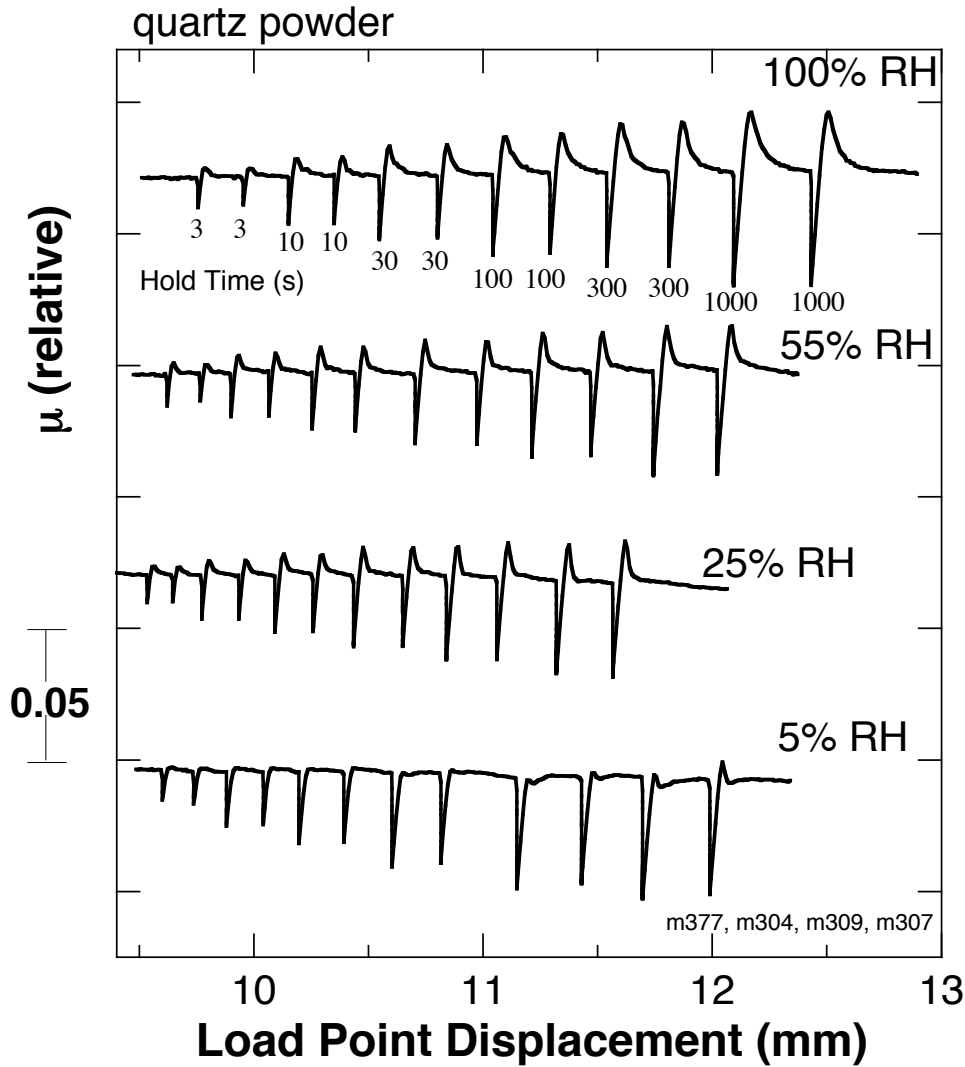
Time dependent friction from time dependent contact area



Dieterich and Kilgore [1994]

Time dependent growth of contact (acrylic plastic)- true static contact

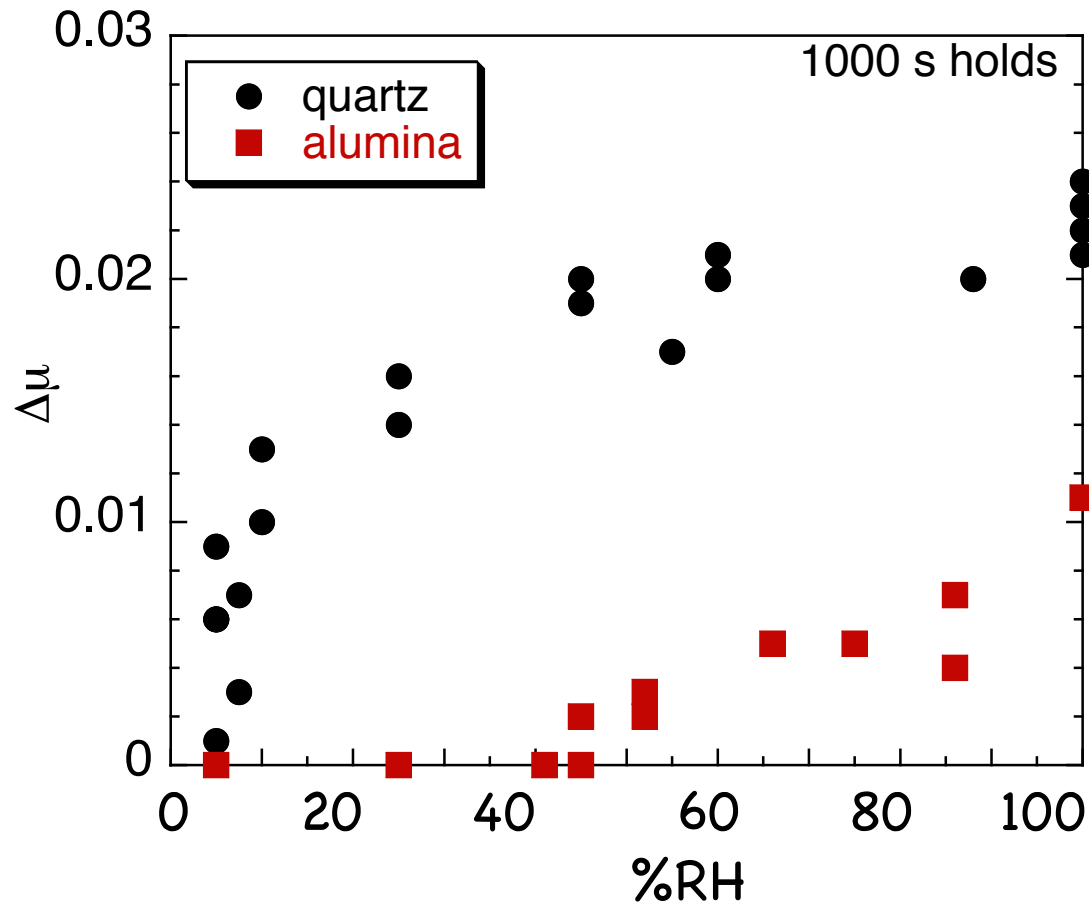
Chemically-Assisted Frictional Aging; Creep at Adhesive Contact Junctions



In-situ Particle Comminution; Production of Fresh Surface Area

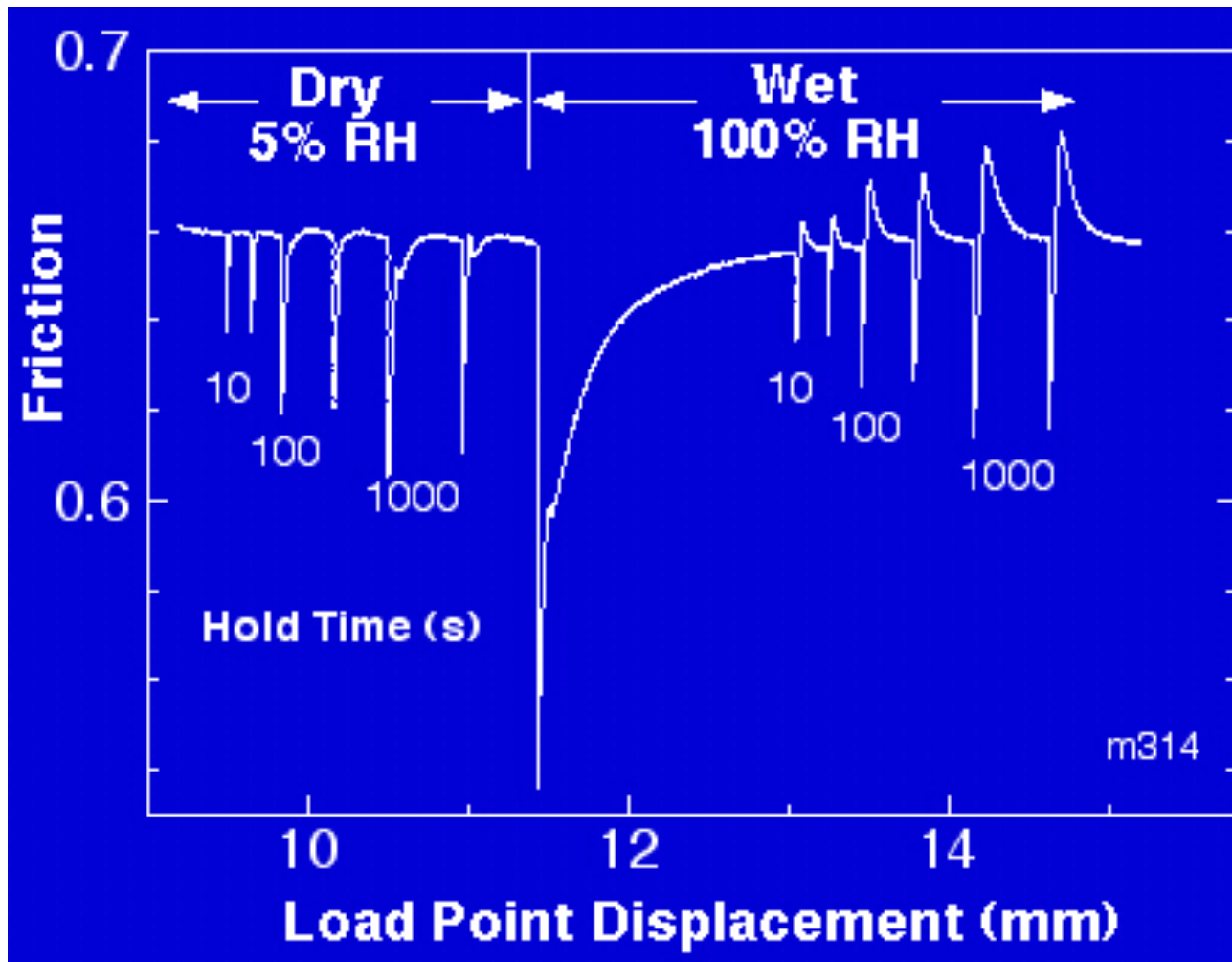
Frye and Marone, JGR 2002

Granular quartz



**Hydrolytic Weakening
causes enhanced rate of
strengthening**

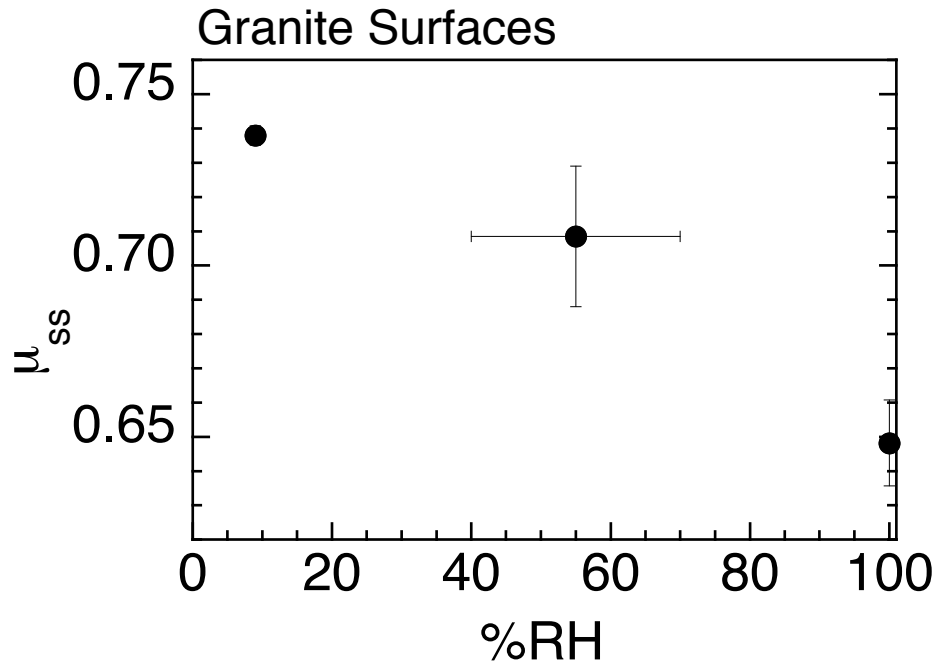
Chemically-Assisted Frictional Aging; Creep at Adhesive Contact Junctions



Hydrolytic Weakening causes enhanced rate of strengthening, but base level frictional strength is unchanged

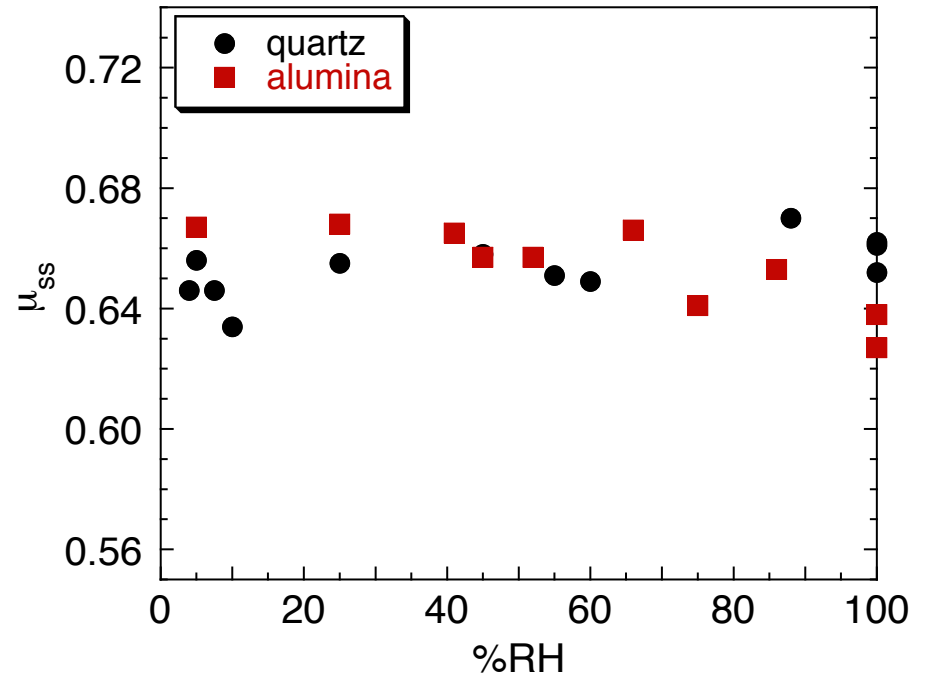
Frye and Marone, JGR 2002

Granite Surfaces



Solid Surfaces: Base level of frictional strength decreases with increasing water content (cf. Dieterich & Conrad, 1984)

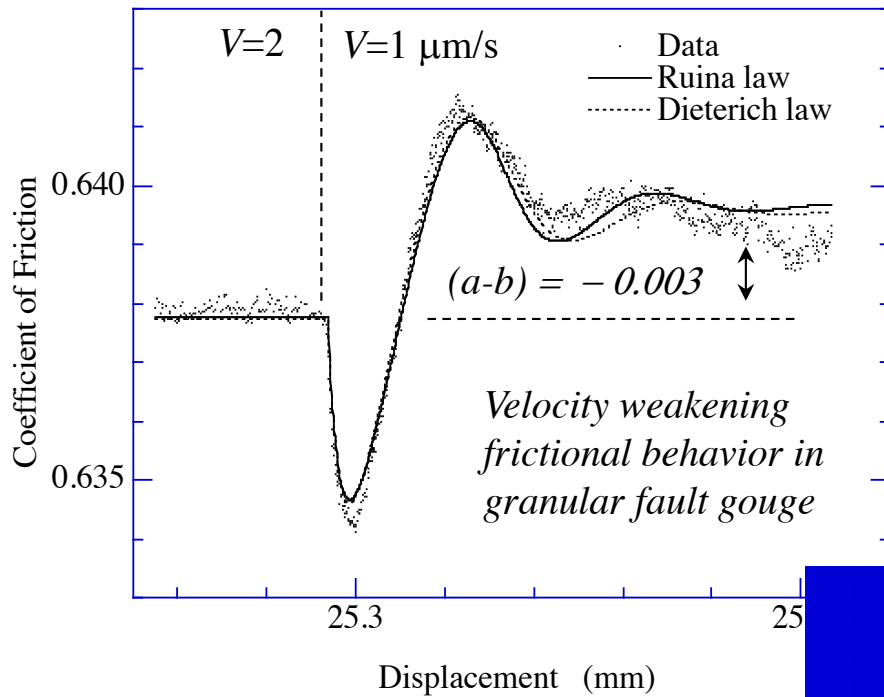
Granular Materials



Granular Materials: Frictional strength is independent of water content

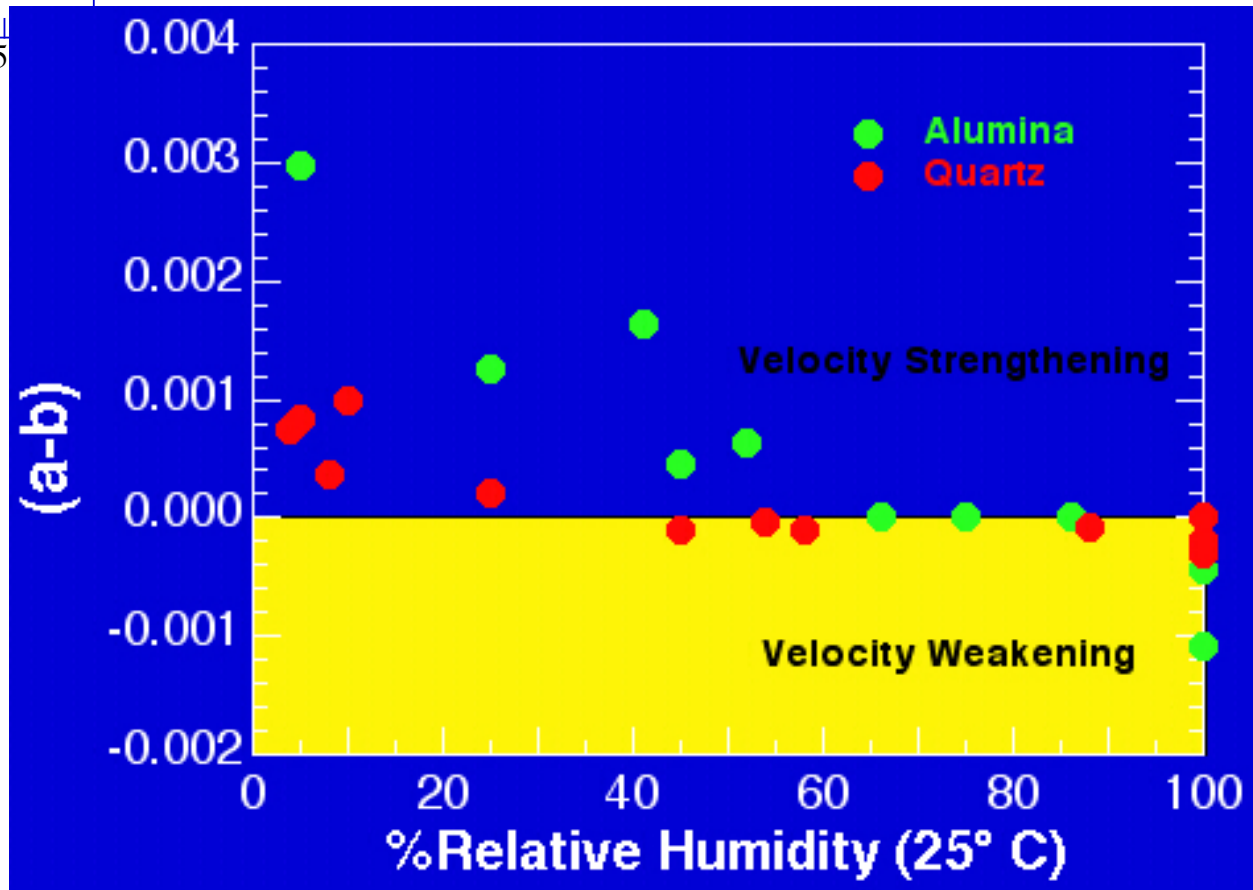
Interpretation: Contact junctions subject to time dependent strengthening or growth, which inhibits sliding, but particle rolling is not affected by these factors.

Empirical laws, based on laboratory friction data



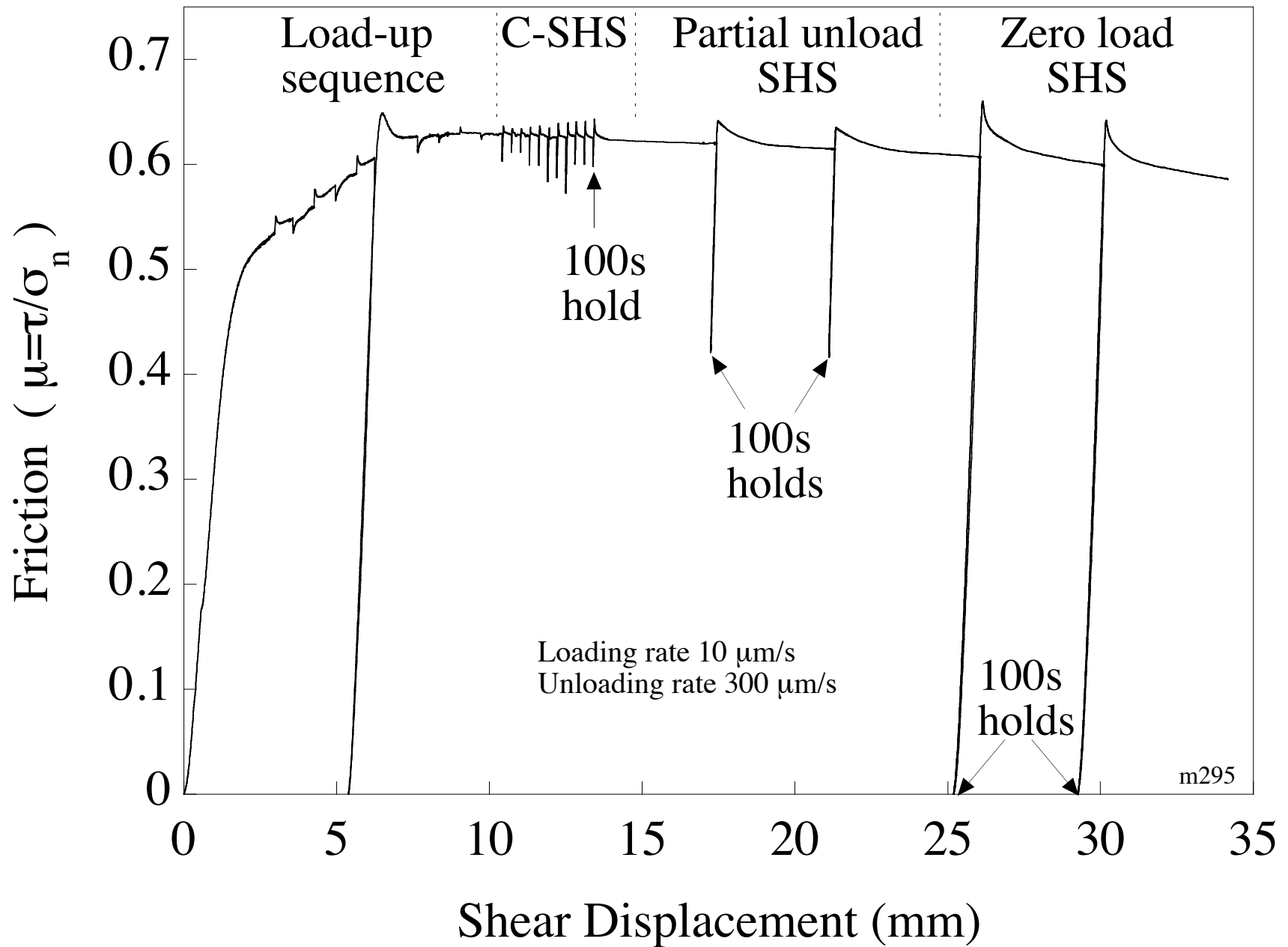
Velocity dependence of steady state friction varies changes from positive to negative. (cf. Tullis and co-workers)

Chemically-assisted creep at adhesive contact junctions



Frye and Marone, JGR 2002

Stresses v. Unstressed Aging



Karner & Marone (GRL 1998, JGR 2001)

100 s holds, Healing rate varies systematically with shear stress

